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General Certificate of Education June 2010

Mathematics

MPC1

Pure Core 1



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Key to mark scheme and abbreviations used in marking

М	mark is for method					
m or dM	mark is dependent on one or more M marks and is for method					
А	mark is dependent on M or m marks and is for accuracy					
В	mark is independent of M or m marks and is for method and accuracy					
E	mark is for explanation					
$\sqrt{100}$ or ft or F	follow through from previous incorrect result	МС	mis-copy			
CAO	correct answer only	MR	mis-read			
CSO	correct solution only	RA	required accuracy			
AWFW	anything which falls within	FW	further work			
AWRT	anything which rounds to	ISW	ignore subsequent work			
ACF	any correct form	FIW	from incorrect work			
AG	answer given	BOD	given benefit of doubt			
SC	special case	WR	work replaced by candidate			
OE	or equivalent	FB	formulae book			
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme			
–x EE	deduct <i>x</i> marks for each error	G	graph			
NMS	no method shown	с	candidate			
PI	possibly implied	sf	significant figure(s)			
SCA	substantially correct approach	dp	decimal place(s)			

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q	Solution	Marks	Total	Comments
-	$y = \frac{14}{3} - \frac{2}{3}x$	M1		Attempt at $y = \dots$
_()	5 5			r r r
	Gradient $AB = -\frac{2}{3}$	A1	2	Condone error in rearranging equation
(b)(i)	y - 7 ="their grad AB"(x-3)	M1		or $2x + 3y = k$ and sub $x = 3, y = 7$
				or $y = mx + c$, $m = their grad AB$ and
				attempt to find <i>c</i> using $x = 3$, $y = 7$
	$y - 7 = -\frac{2}{3}(x - 3)$ OE	A1	2	$2x+3y = 27$, $y = -\frac{2}{3}x+9$ etc
(ii)	$m_1 m_2 = -1$	M1		or <i>negative reciprocal</i> (stated or used PI
	\Rightarrow grad $AD = \frac{3}{2}$	A1√		FT their grad AB
	$y-7=\frac{3}{2}(x-3)$	A1		Any correct equation unsimplified
	$\Rightarrow 3x - 2y + 5 = 0$	A1	4	Integer coefficients; all terms on one side condone different order or multiples. eg $0 = 4y - 6x - 10$
(c)	2x+3y=14 and $5y-x=6$ used			
	with x or y eliminated (generous)	M1		2(5y-6)+3y=14 etc
	x = 4,	A1	3	P(4,2) full more NMS
	y = 2 Total	A1	5 11	B(4,2) full marks NMS
2(a)	$(3 - \sqrt{5})^2 = 9 - 6\sqrt{5} + (\sqrt{5})^2$	M1		Allow one slip in one of these terms
	$=14-6\sqrt{5}$	A1	2	M0 if middle term is omitted
	$(-)^2$			_
(b)	$\frac{\left(3-\sqrt{5}\right)^2}{1+\sqrt{5}} \times \frac{1-\sqrt{5}}{1-\sqrt{5}}$	M1		or $\dots \times \frac{\sqrt{5} - 1}{\sqrt{5} - 1}$
	$14 + 6\sqrt{5}\sqrt{5} - 6\sqrt{5} - 14\sqrt{5}$	1		Europeire di si compositore
	$(=44-20\sqrt{5})$	m1		Expanding <i>their</i> numerator (condone one error or omission)
	(Denominator) = -4	B1		Must be seen as denominator
	$(\text{Answer}) = -11 + 5\sqrt{5}$	A1	4	Accept "answer = $5\sqrt{5} - 11$ "
			6	

Q	Solution	Marks	Total	Comments
3(a)(i)	$p(-3) = (-3)^3 + 7(-3)^2 + 7(-3) - 15$	M1		p(-3) attempted; NOT long division
	= -27 + 63 - 21 - 15			This line alone implies M1
	$p(-3)=0 \implies (x+3 \text{ is}) \text{ factor}$	A1	2	p(-3) shown = 0 plus statement
(ii)	$p(x) = (x+3)(x^2 + px + q)$	M1		Full long division, comparing coefficient or by inspection either $p = 4$ or $q = -5$
	(Quadratic factor) $(x^2 + 4x - 5)$	A1		or M1 A1 for either <i>x</i> –1 or <i>x</i> +5 <i>clearly</i> found using Factor Theorem
	(p(x)=) (x+3)(x-1)(x+5)	A1	3	Must be seen as a product of 3 factors NMS full marks for correct product
				SC B2 for 3 correct factors listed NMS SC B1 for $(x + 3)(x - 1)()$ or $(x + 3)(x + 5)()$ or $(x + 3)(x + 1)(x - 5)$
(b)	$p(2) = 2^3 + 7 \times 2^2 + 7 \times 2 - 15$	M1		NOT long division; must be $p(2)$
	or $(2+3)(2-1)(2+5)$			May use "their" product of factors
	(Remainder) = 35	Alcso	2	
(c)(i)	p(-1) = -16; p(0) = -15 $\Rightarrow p(-1) < p(0)$	B1	1	Values must be evaluated correctly
(ii)				
	У ↑ /	B1		y- intercept -15 marked or (0,-15) state
		M1		Cubic graph – 1 max, 1 min
	-5 -3 1 x	A1		\wedge shape with -5, -3, 1 marked
	Cannot score M1A0A1 but can score	A1	4	Graph correct with minimum point to le of y-axis and going beyond both –5 and Previous A1 must be scored
	B0M1A1A1			rievious A1 must de scoled
	Total		12	

Q	Solution	Marks	Total	Comments
	r ⁵ 8	M1		One term correct
4(a)(i)	$\frac{x^5}{5} - \frac{8}{2}x^2 + 9x$	A1		Another term correct
		A1		All correct (may have $+ c$)
	$\frac{32}{5} - 16 + 18$ = $8\frac{2}{5}$	m1		F(2) attempted
	$=8\frac{2}{5}$	A1	5	$\frac{42}{5}$, 8.4
(ii)	Shaded area $= 18 - `their integral'$	M1		PI by 18 – (a)(i) NMS
	$=9\frac{3}{5}$	A1	2	$\frac{48}{5}$, 9.6 NMS full marks
	dy 13 a	M1		One term correct
(b)(i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 4x^3 - 8$	A1		All correct (no $+ c$ etc)
	$x=1 \Longrightarrow \frac{dy}{dx}=4-8$	m1		sub $x = 1$ into their $\frac{dy}{dx}$
	(Gradient of curve $) = -4$	A1cso	4	No ISW
(ii)	$y-2 = -4(x-1); y = -4x+c, \ c = 6$	B1√	1	any correct form ; FT <i>their</i> answer from (b)(i) but must use $x = 1$ and $y = 2$
	Total		12	

Q	Solution	Marks	Total	Comments
5(a)		M1		One term correct LHS
$\mathbf{J}(\mathbf{a})$	$(x+5)^{2} + (y-6)^{2} = 5^{2}$	A1		LHS all correct
		B1	3	RHS correct: condone = 25
(b)(i)	sub $x = -2$, $y = 2$ into circle equation			Circle equation must be correct
	$3^2 + (-4)^2 = 25$			
	\Rightarrow lies on circle	B1	1	Must have concluding statement
(ii)	Grad $PC = -\frac{4}{3}$	B1		Condone $\frac{4}{3}$
	J			-3
	Normal to circle has equation			M0 if tangent attempted or incorrect
	y-6 = 'their gradient PC'(x+5)	M1		coordinates used
	or $y-2 = 'their gradient PC'(x+2)$			
	$y-6=-\frac{4}{3}(x+5)$			Any correct form eg $4x+3y+2=0$
	3	Alcso	3	
	or $y-2 = -\frac{4}{3}(x+2)$	11000	5	$y = -\frac{4}{3}x + c, c = -\frac{2}{3}$
				Alternative 1
(iii)	$PM = \frac{1}{2} \times \text{radius}$	M1		Attempt at $M\left(-\frac{7}{2},4\right)$ with at least one
	_			correct coordinate and PM^2 attempted
	2.5	A 1		$PM^2 = \frac{9}{4} + 4 = \frac{25}{4}$
	= 2.5	Alcso		
	$PO = \sqrt{8}$	B1		$PO^2 = 4 + 4 = 8$
	P is closer to the point M	E1cso	4	Statement following correct values
				Alternative 2
				Attempt at $M\left(-\frac{7}{2}, 4\right)$ with at least one
		(M1)		$\left($
		(correct coordinate and attempt at vector or difference of coordinates
		(A1cso)		$\overrightarrow{PM} = \begin{pmatrix} -1.5\\2 \end{pmatrix}$ OE
		(E1cso)		P is closer to the point M
		(E1)	(4)	Components of their \overrightarrow{PM} and \overrightarrow{OP} considered – <i>totally independent</i> of M1
	Total		11	

PC1 (cont		3.6.3		C (
Q	Solution	Marks	Total	Comments
6(a)(i)	S.A. = $4xy + 5xy + 3xy + 6x^2 + 6x^2$ OE	M1		Condone one slip or omission
	$=12xy+12x^2$	A1		
	$144 = 12xy + 12x^2$			Must see this line
	$\Rightarrow xy + x^2 = 12$	Alcso	3	AG
(ii)	(Volume =) $\frac{1}{2} \times 3x \times 4x \times y$ OE	M1		
	$= 6x^2 \times \frac{(12 - x^2)}{x}$			Must see $(y=)\frac{(12-x^2)}{x}$ or $xy=12-x^2$
	$(V=)72x-6x^3$	A1	2	for A1 AG must be convinced not working back from answer
(b)(i)	$\frac{\mathrm{d}V}{\mathrm{d}x} = 72 - 18x^2$	M1 A1	2	One term correct All correct (no $+ c$ etc)
(ii)	$x = 2 \Longrightarrow \frac{\mathrm{d}V}{\mathrm{d}x} = 72 - 18 \times 2^2$	M1		Substitute $x = 2$ into their $\frac{dV}{dx}$
	$\Rightarrow \frac{dV}{dx} = 72 - 72 = 0$	A1	2	Shown - 0 alus statement
	\Rightarrow stationary (value when $x = 2$)	AI	2	Shown = 0 plus statement Statement may appear first
(c)	$\frac{\mathrm{d}^2 V}{\mathrm{d}x^2} = -36x$	B1√		FT their $\frac{\mathrm{d}V}{\mathrm{d}x}$
	$\frac{\mathrm{d}^2 V}{\mathrm{d}x^2} = -72 \ or \ \text{when } x = 2 \Longrightarrow \frac{\mathrm{d}^2 V}{\mathrm{d}x^2} < 0$			
	⇒maximum	E1√	2	FT their $\frac{d^2V}{dx^2}$ value when $x = 2$
				with appropriate conclusion
	Total		11	

Q	Solution	Marks	Total	Comments
7(a)(i)	$2(x-5)^2$	B1		<i>p</i> = 5
	+ 3	B1	2	<i>q</i> = 3
(ii)	Stating both $(x-5)^2 \ge 0$ and $3 > 0$ $\Rightarrow 2x^2 - 20x + 53 > 0$ or $2(x-5)^2 + 3 > 0$	M1		FT their $p \& q$, but must have $q > 0$
	$\Rightarrow 2x^2 - 20x + 53 = 0$ has no real roots	A1cso	2	Must have statement and correct $p \& q$.
(b)(i)	$b^2 - 4ac = (k+1)^2 - 4k(2k-1)$	M1		Condone one slip (including <i>x</i> is one slip)
	$= -7k^2 + 6k + 1$	A1		Condone recovery from missing brackets Their discriminant ≥ 0 (in terms of <i>k</i>)
	real roots $\Rightarrow b^2 - 4ac \ge 0$ $-7k^2 + 6k + 1 \ge 0$	B1√		Need not be simplified & may earn earlier
	$\Rightarrow 7k^2 - 6k - 1 \leq 0$	Alcso	4	AG (must see sign change)
(ii)	(7k+1)(k-1)	M1		Correct factors or correct use of formula
	Critical values $k = 1, -\frac{1}{7}$	A1		May score M1, A1 for correct critical values seen as part of incorrect final answer with or without working.
	Use of sign diagram or sketch + $+$ $+$ $+$ $+$ $+$ $+$ $+$ $+$ $+$	M1		If previous A1 earned, sign diagram or sketch must be correct for M1
	$-\frac{1}{7}$ 1 -			Otherwise M1 may be earned for an attempt at the sketch or sign diagram using <i>their</i> critical values.
	$-\frac{1}{7} \leqslant k \leqslant 1$	A1	4	$\left(-\frac{1}{7} < k < 1\right), \left(k \ge -\frac{1}{7} \text{ OR } k \le 1\right),$
	Full marks for correct answer NMS			$\left(k \ge -\frac{1}{7}, k \le 1\right)$ score M1A1M1A0
	Condone $-\frac{2}{14}$ throughout			Answer only of $k < -\frac{1}{7}$, $k < 1$ etc
	Condone $k \ge -\frac{1}{7}$ AND $k \le 1$ for full			scores M1, A1, M0 since the critical values are evident.
	7 marks			Answer only of $\frac{1}{7} \leq k \leq 1$ etc
	Take their final line as their answer.			scores M0, M0 since the critical values are not both correct.
	Total		12	
	TOTAL		75	